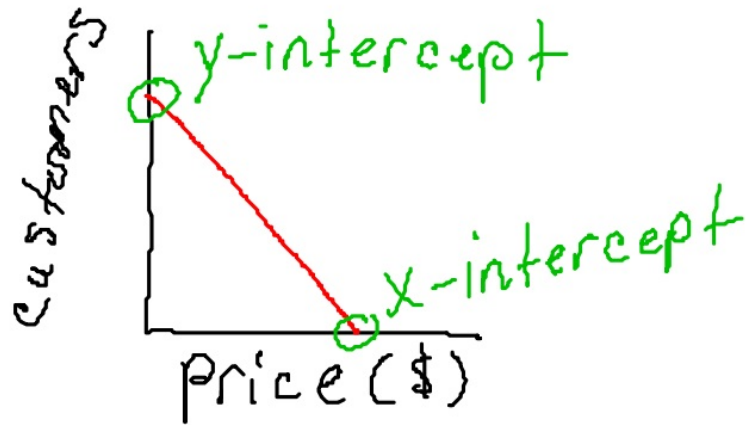


Chapter 4: Functions, Relations, and Transformations

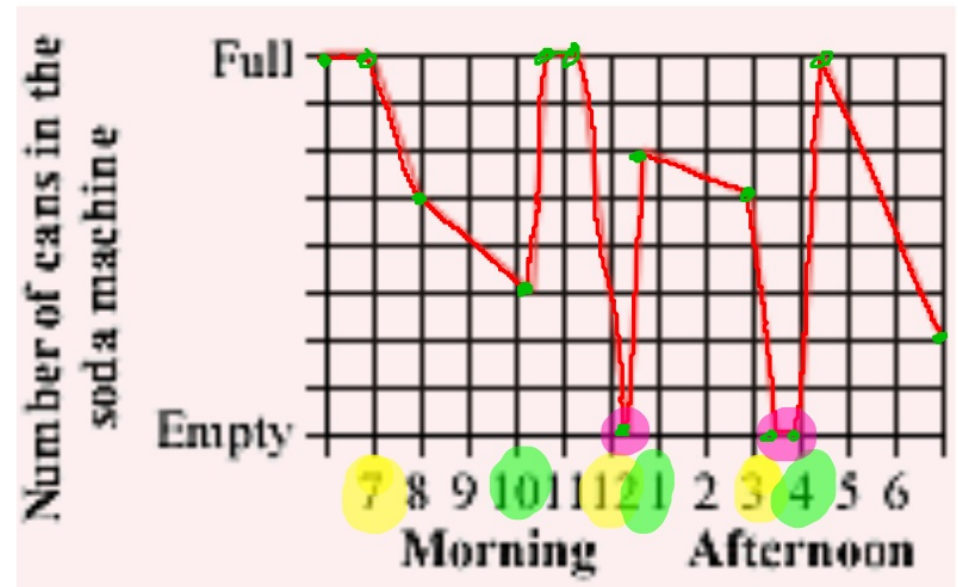
5/9

4.1 Interpreting Graphs p. 172

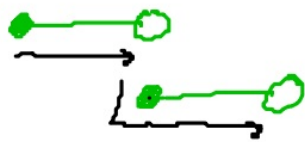


Independent var (x-axis)
we control

Dependent var. (y-axis)
We measure



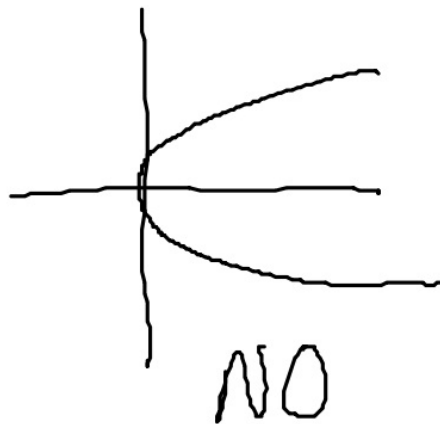
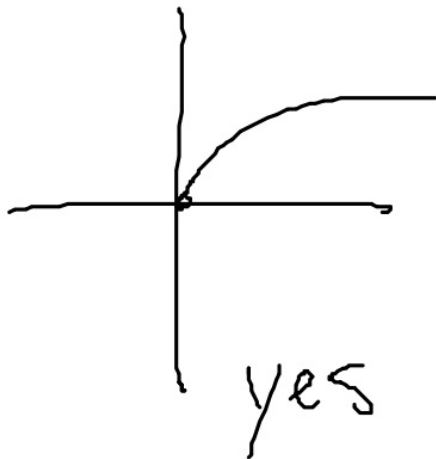
add 2nd machine
fill at 12:00
fill full at 12:00
fill at 3:00 (full)
evening fill to 5:30

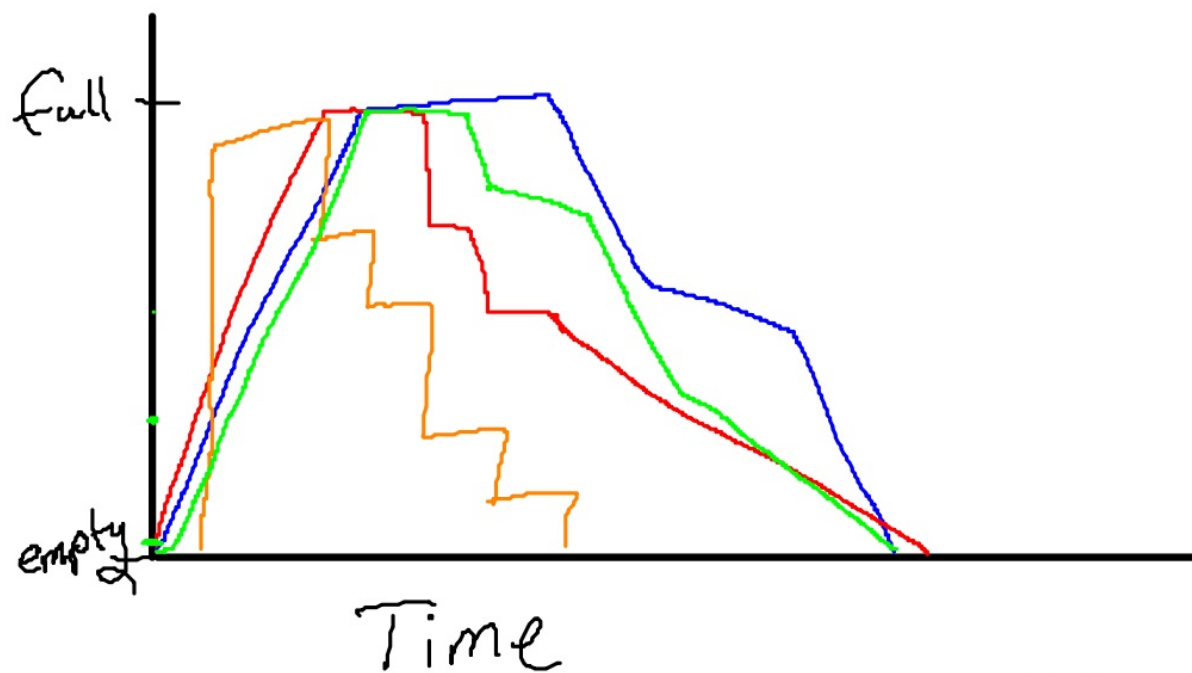


- we have data
- we have no data

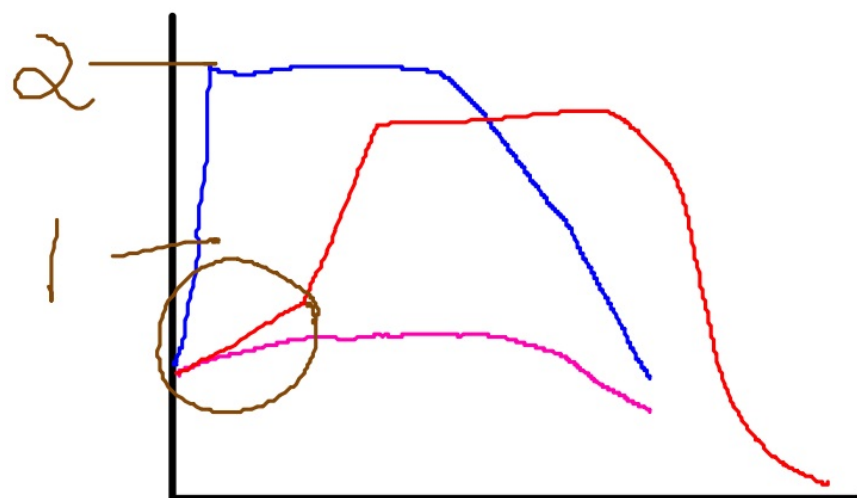
function - graph passes the vertical line test
(hits at most once)

- for every x there is at most
one y





VA
AF
AB
mm

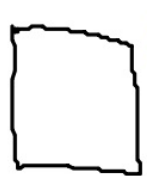


pp. 175-176
#1-5 5/10

AF
VA

function - graph passes vertical line test
- for every X there is at most one Y

relation - how 2 variables relate

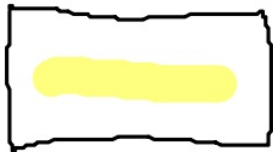


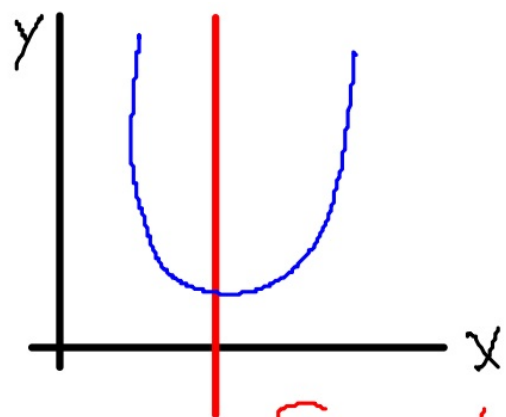
$4 \times 90^\circ \angle$

sides \parallel

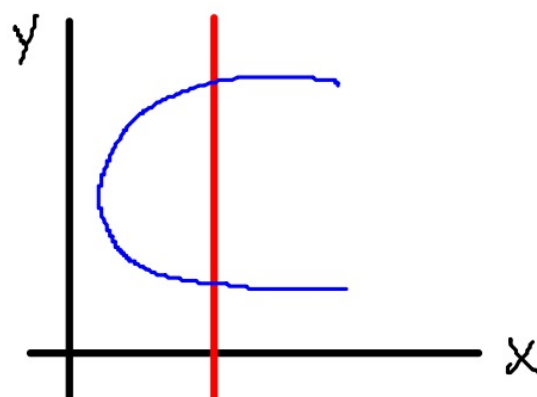
4 sides

sides = length





Function



NOT A FUNCTION

$(3, 4)$ $(5, 2)$ $(7, 0)$ $(8, -1)$ ✓

$(3, 4)$ $(3, 2)$ $(2, 0)$ $(5, 1)$ ✗

$(3, 4)$ $(5, 4)$ $(12, 4)$ $(-1, 4)$ ✓

Function notation

$y = f(x)$ "y equals f of x"

$$y = \frac{(x-2)(x+3)}{\sqrt{x^2-16}} = f(x)$$

$$f(2) = \frac{0.5}{\sqrt{-12}} = 0$$

$f(2)$ solve for y when $x=2$

$g(x)$

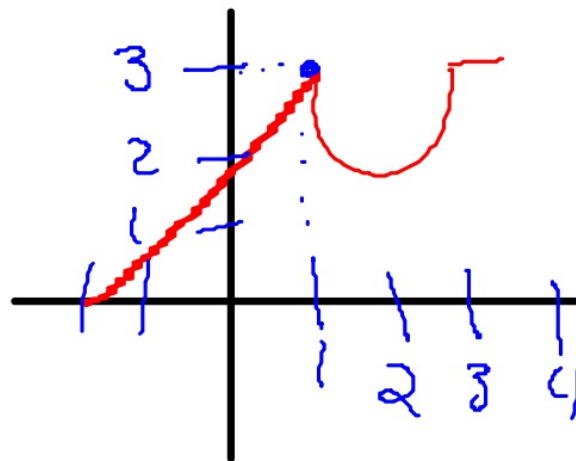
$$f(x) = \frac{2x+5}{x-3}$$

$$f(8) = \frac{2(8)+5}{8-3} = \frac{21}{5} = 4\frac{1}{5} = 4.2$$

$$f(-7) = \frac{2(-7)+5}{-7-3} = \frac{-9}{-10} = 0.9$$

$$g(1) = 3$$

$$g(-2) = 0$$



Inv. a Yes d NO yes g NO
^{domain}
 a- $1 \leq x \leq 4$ b NO e Yes yes h yes
 $1 \leq y \leq 4$
^{range}
 x from -1 to 4 c Yes f NO i yes yes

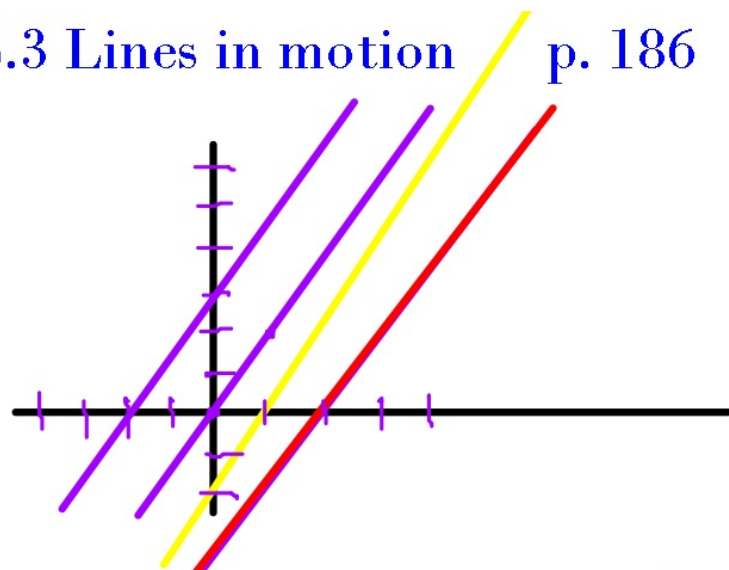
domain - the values used for x

range - the values used for y

$1 < x < 4$ x between 1 and 4

$1 < x \leq 4$

4.3 Lines in motion p. 186



$$y = ax + b$$

5/16

$$y = y_1 + b(x - x_1)$$

$$y = 2x - 4 + 2 = 2x - 2$$

$$y = 2x \quad \text{moved/translated up 3 units}$$

$$y = 2x + 3$$

$$y = 2x - 4$$

down 4 units

$$y = 2x - 4$$

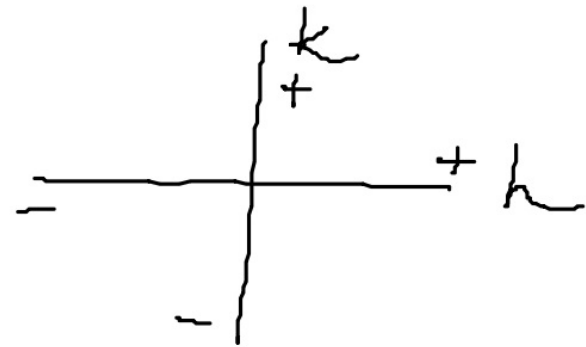
$$y = 2x - 4 \quad \text{right 2 units}$$

$$y = 2x - 2 \quad \text{right 2 units + up 2 units}$$

h - horizontal movement

k - Vertical movement

Vertical \updownarrow
horizontal \leftrightarrow



$$(y-k) = a(x-h) + b$$

$$y = f(x) \quad y = f(x-h) + k$$

right 2 units

up 2 units

down 2 left 2

$$y = f(x-2) + 0$$

$$y = f(x-0) + 2$$

$$y = f(x+2) - 2$$

$$y = f(x-2) + 2$$

to the right 4 and down 3

$$y = f(x-4) + -3$$

$$f(x) = 2x + 6$$

$$y = 2(x-4) + 6 + -3$$

$$y = 2x - 8 + 6 - 3$$

$$y = 2x - 5$$

move down 11

$$f(x) = 3x + 6$$

$$y = 3(x-4) + 6 - 3$$

$$y = 3x - 12 + 6 - 3$$

$$y = 3x - 9$$

move down 15

slope matters

$$f(x) = 2x$$

How is $f(x) = 4 + 2(x - \underline{3})$ a translation?

$$h = 3 \quad \text{right } 3$$

$$k = 4 \quad \text{up } 4$$

$$(x - \underline{h})$$

$$y = f(x - h) + k$$

$$y = 4 + 2(x - 3)$$

$$(y - 4) = 2(x - 3)$$

$$(y - k) = a(x - h)$$

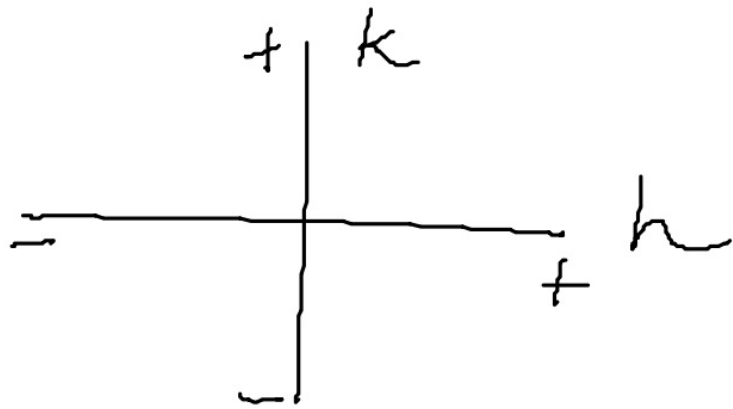
p. 189

#1-5

$$f(x) = x + 7$$

$$f(x + 2) = (x + 2) + 7$$

$$f(3) = 3 + 7$$



$$y = a(x-h) + k$$

$$f(x) = -2x$$

$$\begin{aligned} f(x+3) &= -2(x+3) \\ &= -2x - 6 \end{aligned}$$

Linear

#1

non-linear

arithmetic

geometric

shifted geometric

terms

Sequence

u_0

u_n

u_{n-1}

recursive formula

decreases
Value

#2

Calculate the value of a car
in 5 years (recursive formula)

$$U_0 =$$

$$U_n = U_{n-1} (1 - \% \text{ decrease})^{\text{time}}$$

where $n \geq$

Five number summary

3 + 4

Range

Interquartile Range (IQR)

box plot

skewed (left or right)

Symmetric

mean

Standard deviation

percentile rank